

# Integrated Information: A Formulation of Dynamical Complexity for Neuronal and Artificial Systems

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## Motivation:

- A **global complexity** measure that simultaneously takes into account network structure and dynamics
- Useful for calibrating **complexity of brain states** associated to rest and behavior
- A **clinical measure** of consciousness, cognition & volition
- How does one compare **complexity of biological agents** such as bacteria, bees, C. elegans, primates, humans, etc. to **AI agents** such as deep neural nets, multi-agent robots, Siri, Watson, etc.?
- How can one generalize wakefulness & awareness for non-biological systems to obtain **scales of consciousness** for artificial systems?

## Mathematical Formulation:

The information gain following a state transition equals reduction in uncertainty about initial state  $\mathbf{X}_0$ . Effective information is defined as the subset of the above that is generated by the system as a whole and is given by the **Kullback-Leibler Divergence** between the multivariate conditional distribution of the system versus the joint independent composite of its parts

$$\Phi_{P \rightarrow r}(\mathbf{X}_0 \rightarrow \mathbf{X}_1 = \mathbf{x}') = D_{KL} \left( P_{\mathbf{X}_0 | \mathbf{X}_1 = \mathbf{x}'} \parallel \prod_{k=1}^r P_{M_0^k | M_1^k = \mathbf{m}'} \right)$$

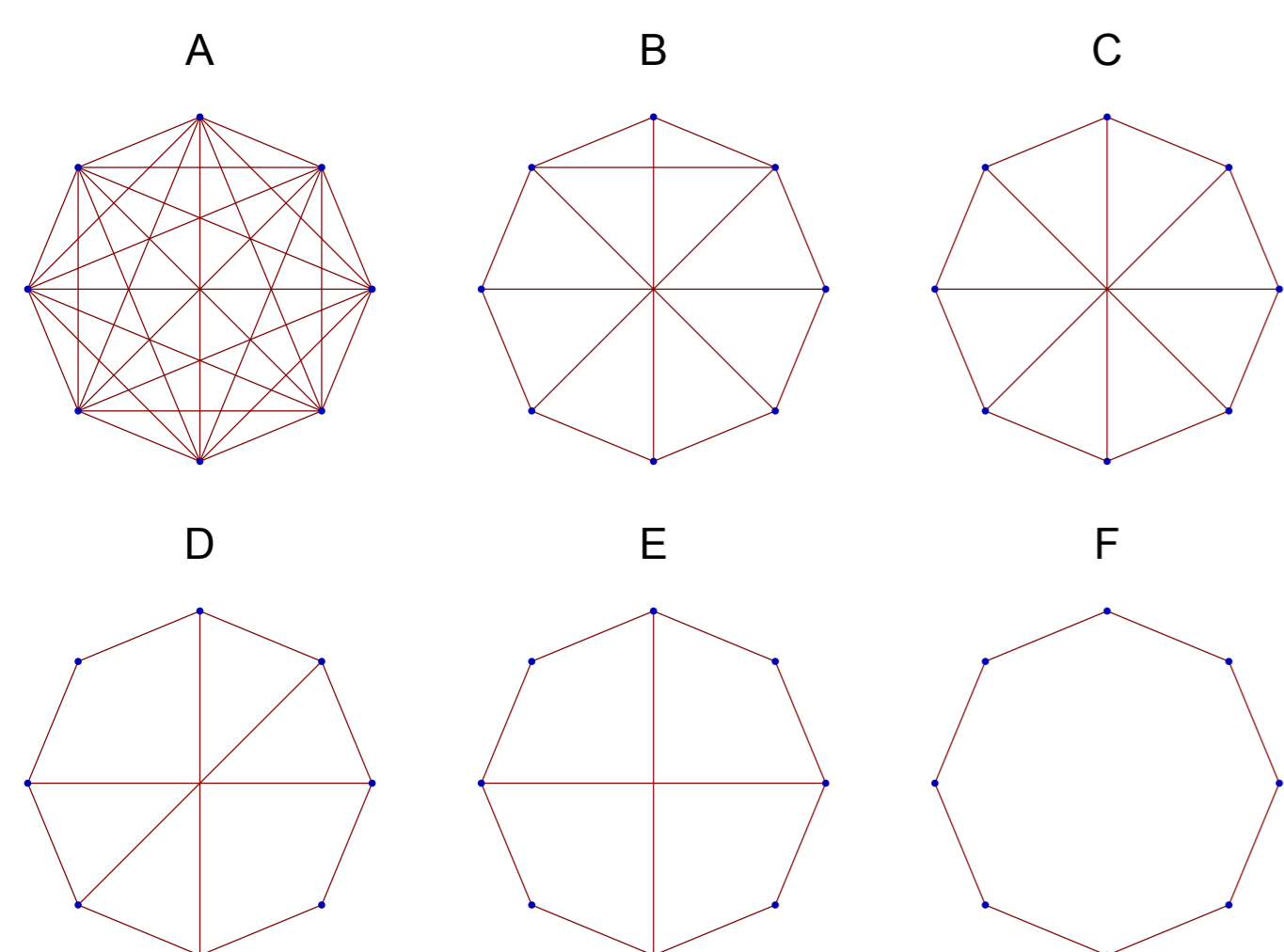
Network states:  $\mathbf{X}_{t_0} = \begin{pmatrix} x_{1t_0} \\ \vdots \\ x_{nt_0} \end{pmatrix} \mapsto \mathbf{X}_{t_1} = \begin{pmatrix} x_{1t_1} \\ \vdots \\ x_{nt_1} \end{pmatrix}$

Dynamical model:  $\mathbf{X}_{t_1} = \mathcal{A} \mathbf{X}_{t_0} + \mathcal{E}$  (Linear Dynamics with Noise)

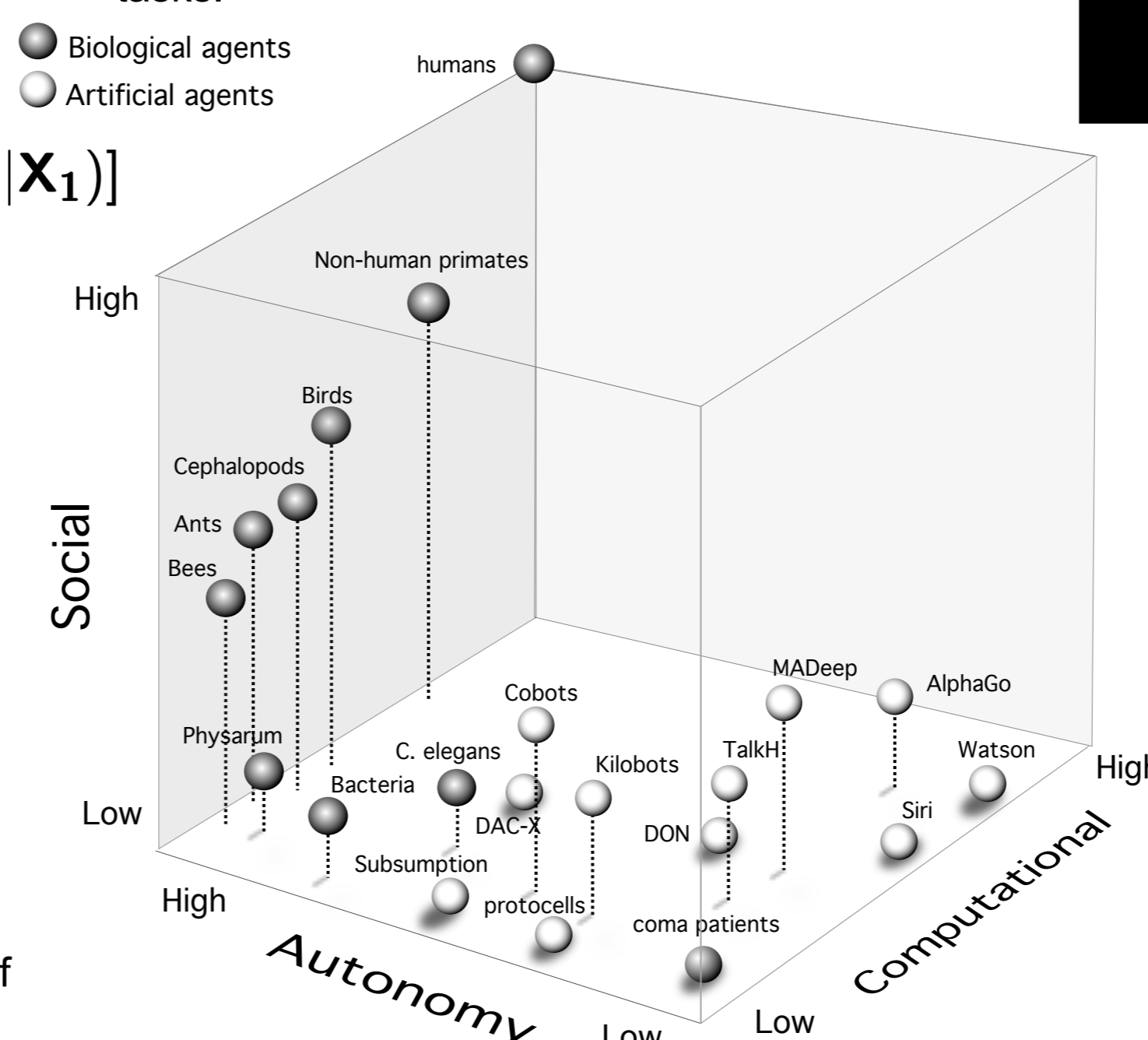
$\mathbf{X}_0 \sim \mathcal{N}(\bar{\mathbf{x}}_0, \Sigma(\mathbf{X}_0))$      $\mathbf{X}_1 \sim \mathcal{N}(\bar{\mathbf{x}}_1, \Sigma(\mathbf{X}_1))$  (Gaussian variables)

Conditional entropy:  $\mathbf{H}(\mathbf{X}_0 | \mathbf{X}_1) = \frac{1}{2} n \log(2\pi e) - \frac{1}{2} \log[\det \Sigma(\mathbf{X}_0 | \mathbf{X}_1)]$

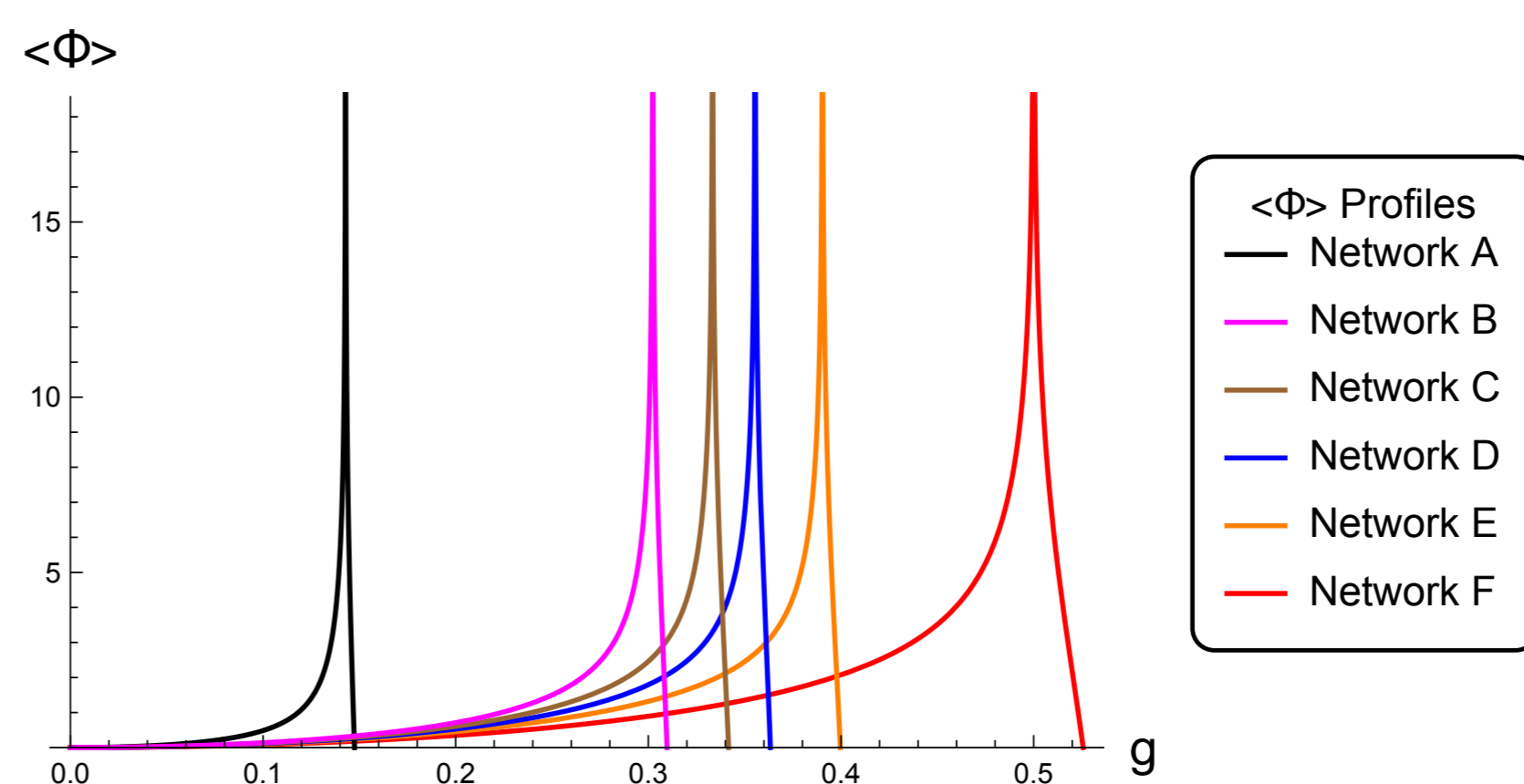
$$\langle \Phi \rangle_{P \rightarrow r}(\mathbf{X}_0 \rightarrow \mathbf{X}_1) = -\mathbf{H}(\mathbf{X}_0 | \mathbf{X}_1) + \sum_{k=1}^r \mathbf{H}(M_0^k | M_1^k)$$



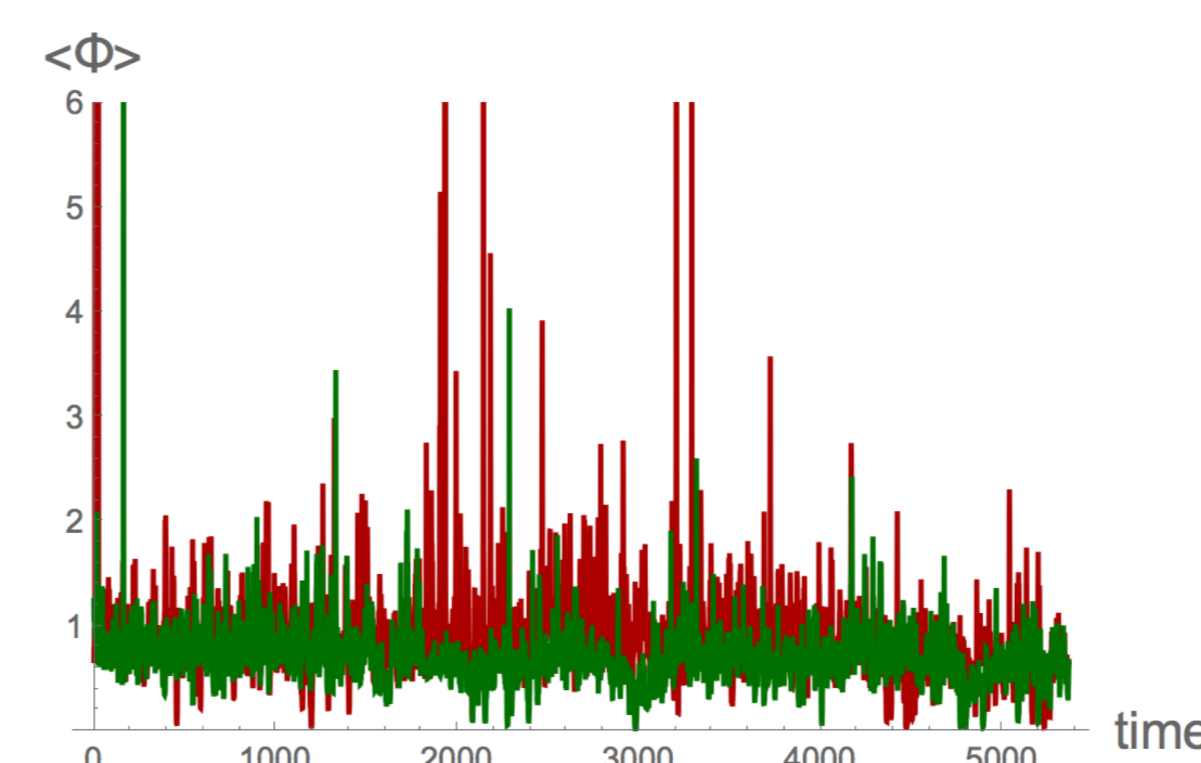
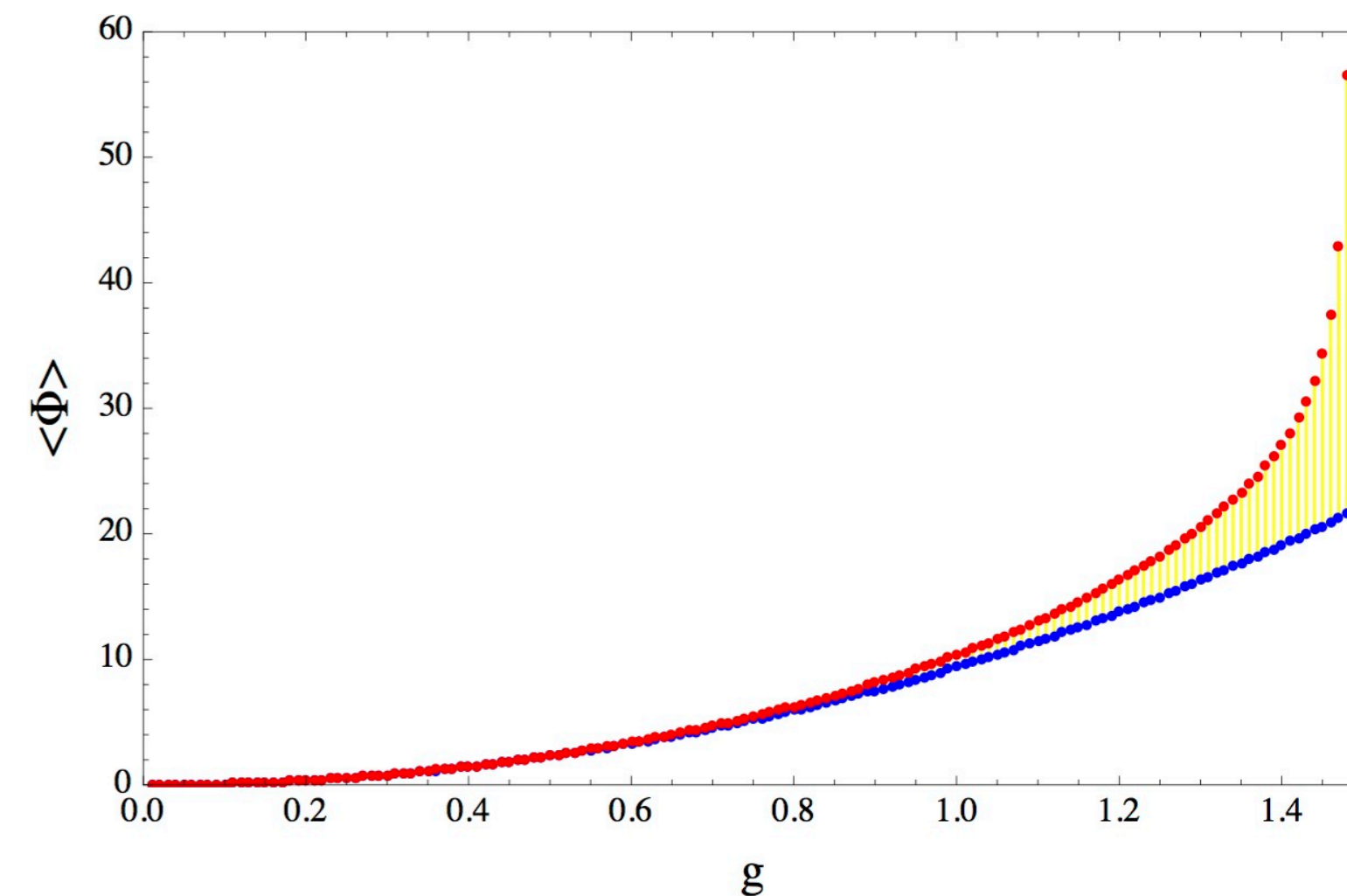
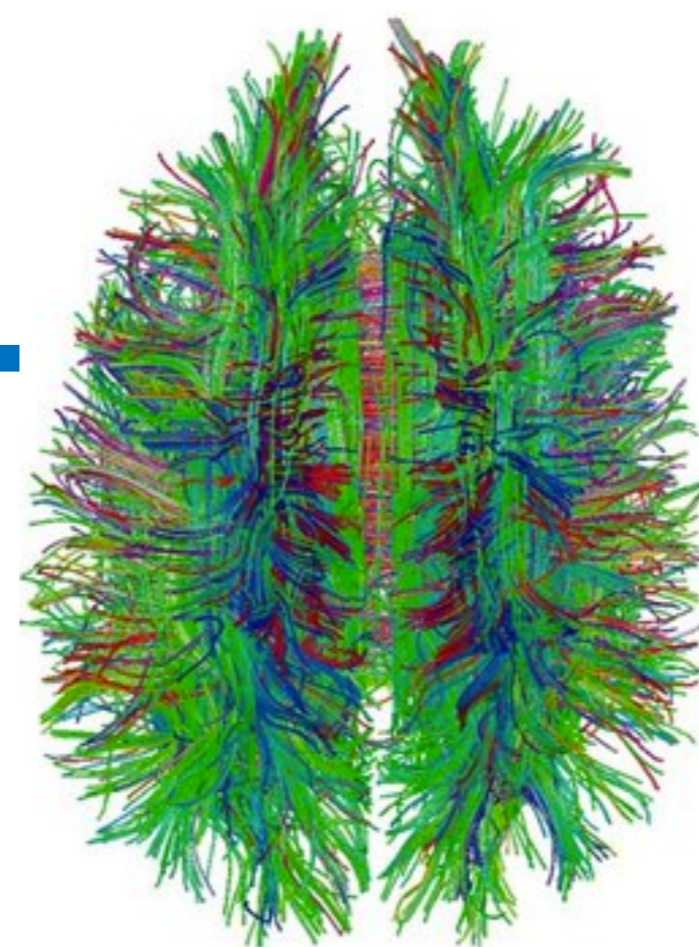
**Figures: (Left):** Six network topologies upon which we apply the above formulation. **(Right):** The morphospace of consciousness showing a taxonomy of biological and artificial agents using three kinds of complexity scales.



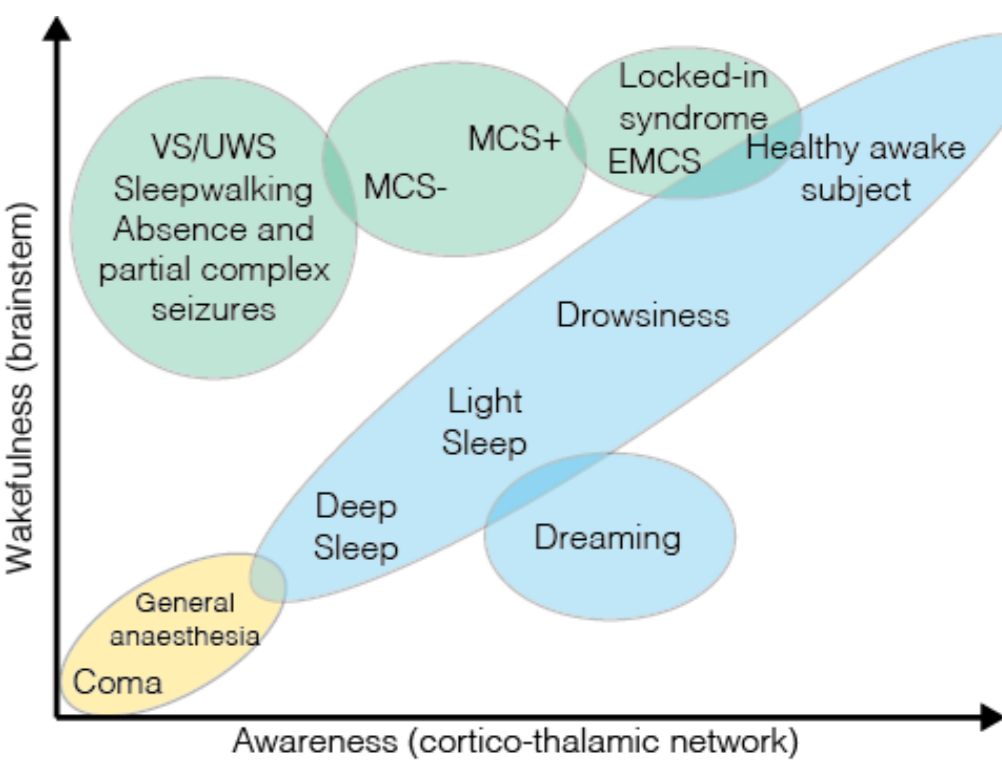
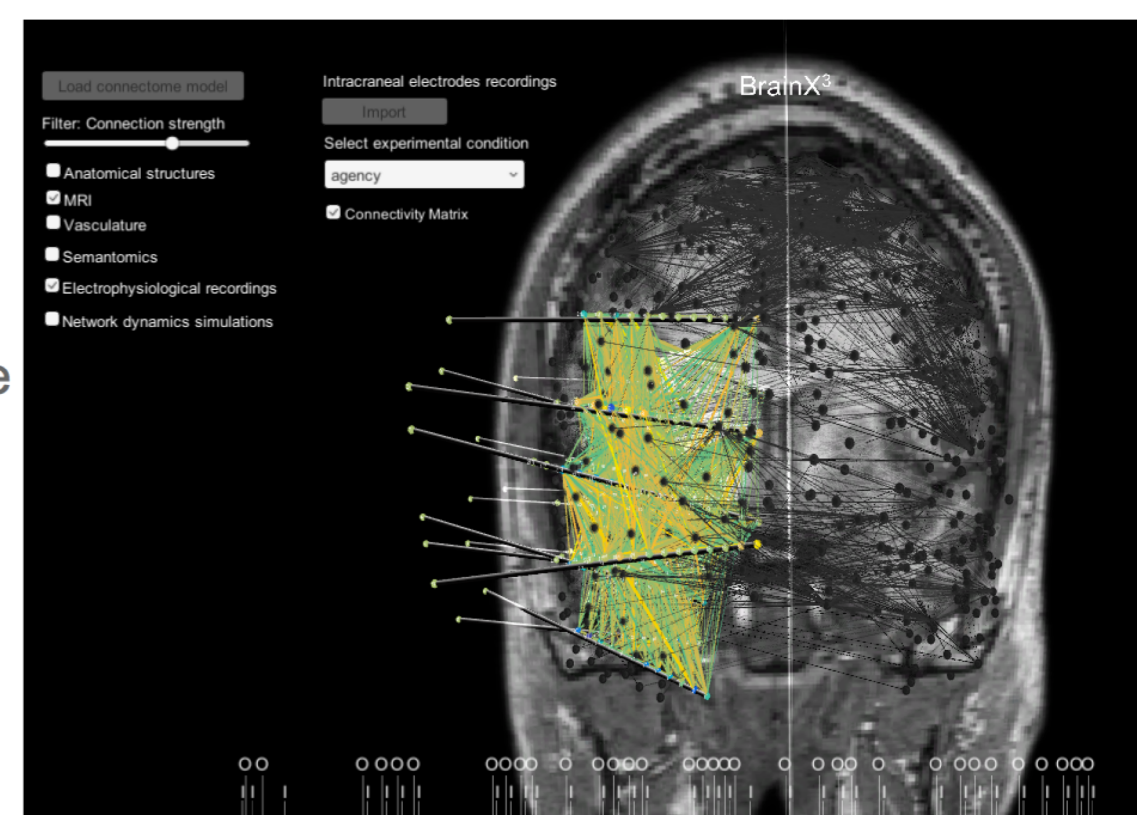
## Results:



**Figures: (Left)** Phi profiles for the 6 networks shown below. Stable solutions until couplings hit critical point showing high phi near criticality. **(Below):** Tractography data from the human connectome (Hagmann 2008) and corresponding phi profile for data vs. randomized network.



**Figures: (Right):** FC from epilepsy patients using iEEG recordings. **(Top):** Temporal phi profiles from FCs obtained in active vs. passive navigation tasks.



**Figures: (Top)** Clinical classification of disorders of consciousness (DoC) based on wakefulness & awareness (Laureys 2005).

## Conclusions:

- An analytic framework for computing integrated information for large biological networks
- High phi near the edge of instability
- As a clinical measure of cognitive complexity
- Generalization to complexity of AI systems

**References:** [1] Arsiwalla, X. D., & Verschure, P. F. (2016). The Global Dynamical Complexity of the Human Brain Network. *Applied Network Science*, 1(1), 16.  
[2] Arsiwalla, X. D., Sole, R., Moulin-Frier, C., Herreros, I., Sanchez-Fibla, M., & Verschure, P. (2017). The Morphospace of Consciousness. *arXiv:1705.11190*.  
[3] Arsiwalla, X. D., Pacheco, D., Principe, A., Rocamora, R., & Verschure, P. F. (2018). A Temporal Estimate of Integrated Information for Intracranial Functional Connectivity. ICANN 2018, Springer.