

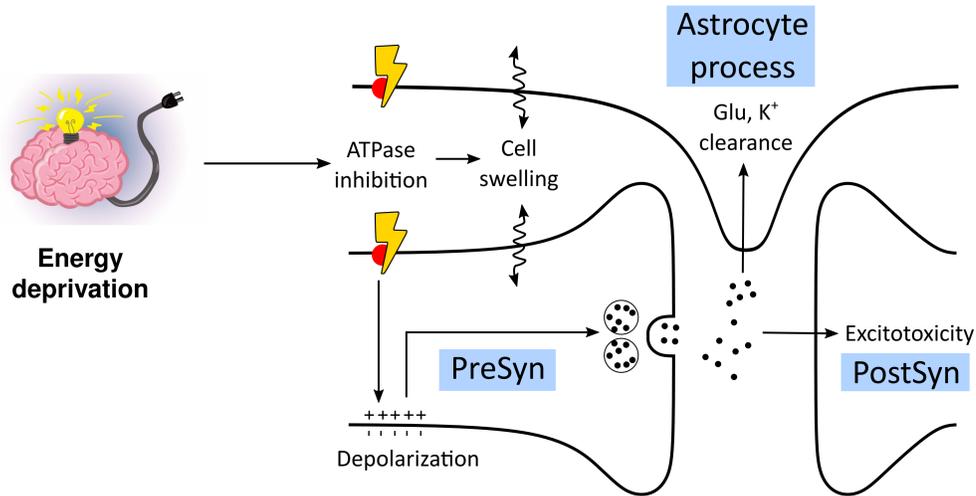
# The energy deprived tripartite synapse: a biophysical model

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## Pathways to pathology during energy deprivation

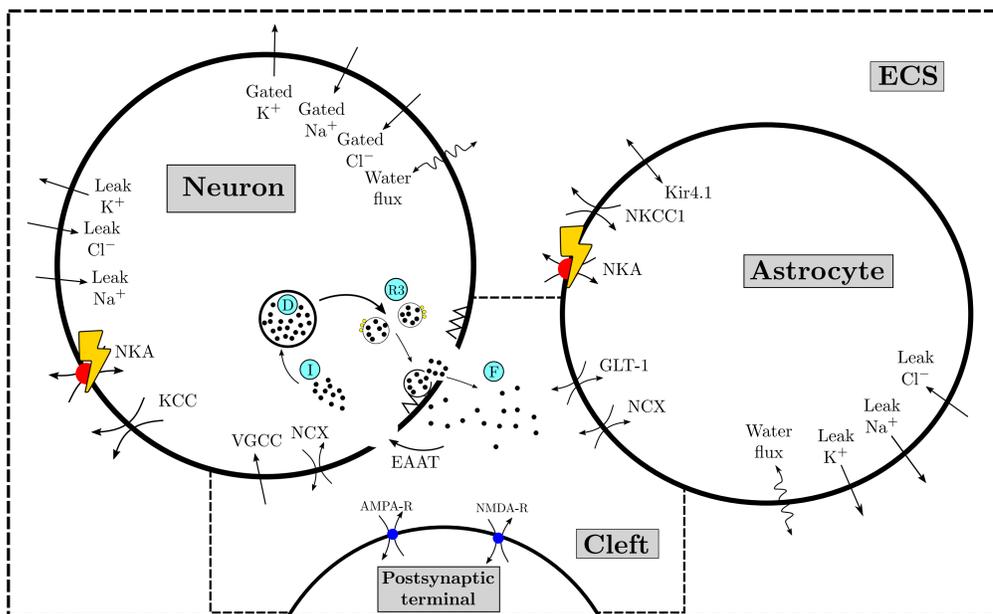
Energy deprivation to the nervous system occurs during **ischemic stroke**, which is one the leading causes of death. The epicenter of physiological breakdown is at the **tripartite synapse**.



### Goal

Describe **transitions** between normal and pathological states at energy deprived tripartite synapses by formulating a **biophysical model**.

## Biophysical model of ion and volume dynamics

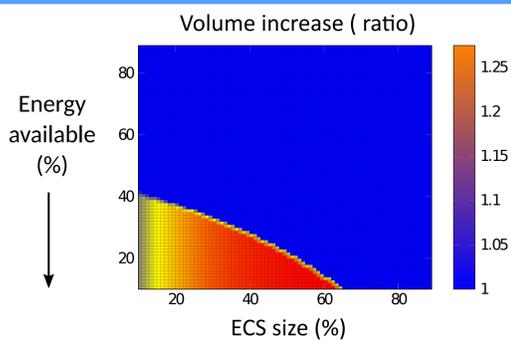


- Dynamics of **five ions: Na<sup>+</sup>, K<sup>+</sup>, Cl<sup>-</sup>, Glu and Ca<sup>2+</sup>**.
- Synaptic terminal + soma → one compartment
- Mass conservation, electroneutrality
- Calibrated to in-vitro ischemia experiments [1].

$$\begin{cases} \frac{d}{dt} N_X^i = -z_X \frac{1}{F} \left( \sum_j I_{X,i}^j + \sum_X I_{X,i}^{ATPase} \right), \\ \frac{d}{dt} Vol_i = \lambda_i \sum_{X,Y} ([X]_i - [Y]_e), \\ \frac{d}{dt} q = \alpha_q (1 - q) - \beta_q q, \\ \sum_{X,i} z_X N_X^i = 0, \\ \sum_i N_X^i = C_X = \text{constant}. \end{cases}$$

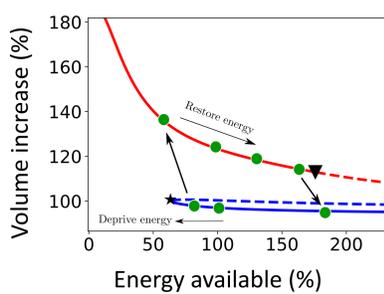
$N_X^i$  = Moles of ion X in compartment i  
 i = {Neuron, Astrocyte, PreSyn}  
 q = Gating variables  
 X = {Na<sup>+</sup>, K<sup>+</sup>, Cl<sup>-</sup>, Ca<sup>2+</sup>, Glu}  
 $I_{X,i}^j$  = Current/Flux of type j w.r.t. ion X in

## Key results



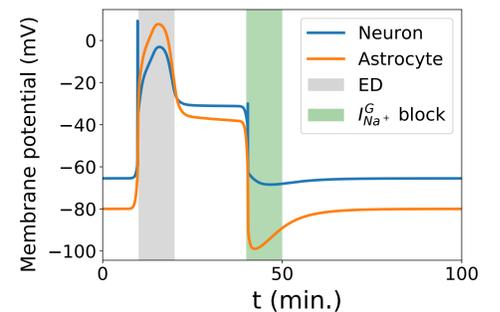
### Cell swelling

Smaller extracellular spaces are more vulnerable to ischemic injury. This may explain experiments in [2].



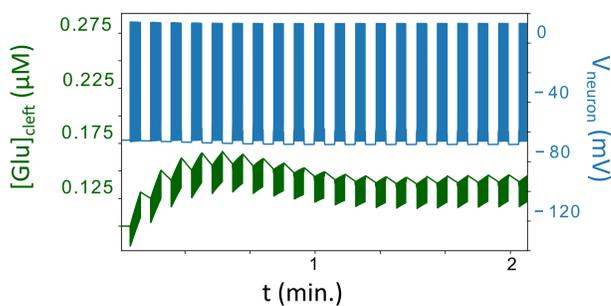
### Bistability

The synapse sustains ischemic injury upto an extent, but needs overpowered pumps to recover.



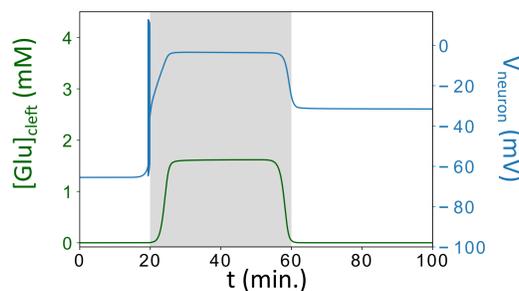
### Depolarization

Blocking transient Na<sup>+</sup> current allows the system to recover back to a normal state, as first suggested in [3].



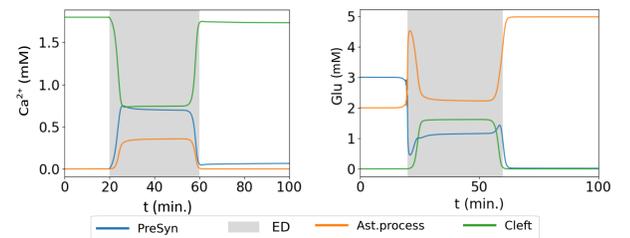
### Healthy synapse

Healthy synaptic transmission is modeled by steady buildup of Glu in the cleft driven by square wave input.



### Excitotoxicity

Toxic buildup of cleft Glu (1mM) occurs in energy deprived synapses which show anoxic oscillations before depolarization block.



### PreSyn failure

Post energy deprivation, presynaptic Glu is depleted, leaving the synapses damaged. Ca<sup>2+</sup> recovers.

## References

- [1] Gerkau, N.J. et al. "Reverse NCX attenuates cellular sodium loading in metabolically compromised cortex." *Cerebral Cortex* (2018) 28(12): 4264-4280.  
 [2] Brisson, C. D. and Andrew, R. D. "A neuronal population in hypothalamus that dramatically resists acute ischemic injury compared to neocortex." *Journal of Neurophysiology* (2002) 108(2): 419-303  
 [3] Dijkstra, K. et al. "A biophysical model for cytotoxic cell swelling." *Journal of Neuroscience* (2016) 36(47): 11881-11890